

Course Name: **A Level (1<sup>st</sup> Sem)**

Subject : **Introduction to DBMS**

Topic: **DB Normalization – Lossless Join Decomposition**  
(Part 12)

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### Database Normalization – Lossless Join Decomposition

Suppose a relational schema R is decomposed into two relations R1 and R2, then this decomposition is considered as **lossless decomposition** if there is no loss of information after decomposition. This property is also known as **lossless join decomposition**.

More technically, we can say that the result of natural join of R1 and R2 are same as R i.e. no extra or less tuple is generated in natural join of R1 and R2.

$$\pi_{\text{Attributes}}(R1) \bowtie \pi_{\text{Attributes}}(R2) = \pi_{\text{Attributes}}(R)$$

It is mandatory property and must always hold while decomposing of table.

The decomposition of R into R1 and R2 always will be lossless, if and only if, all the following three conditions hold true:

1.  $\text{Attribute}(R1) \cup \text{Attribute}(R2) = \text{Attribute}(R)$
2.  $\text{Attribute}(R1) \cap \text{Attribute}(R2) \neq \emptyset$
3. The common attribute(s) between R1 and R2 must be candidate key either in R1 or in R2 i.e.

$$\text{Attribute}(R1) \cap \text{Attribute}(R2) \rightarrow \text{Attribute}(R)$$

$$\text{Attribute}(R1) \cap \text{Attribute}(R2) \rightarrow \text{Attribute}(R)$$

If the decomposition does not follow above three conditions then it is called **lossy decomposition** or **lossy-join decomposition**.

Consider a relation **R** (emp\_id, emp\_name, emp\_dob, dept\_id, dept\_name, dept\_location)

Now, it is divided into:

**R1** (emp\_id, emp\_name, emp\_dob, dept\_id)

**R2** (dept\_id, dept\_name, dept\_location)

If it is lossless join decomposition then it has to follow all the above mentioned three conditions:

- 1- Union of attributes R1 and attributes R2 is equal to attributes of R
- 2- The intersection of attributes R1 and attributes R2 is not null. It is dept\_id.
- 3- The common attribute between R1 and R2 (dept\_id) is the candidate key in R2.

dept\_id  $\rightarrow$  dept\_name, dept\_location

Therefore, It concludes that above decomposition of **R1**(emp\_id, emp\_name, emp\_dob, dept\_id) and **R2** ( dept\_id, dept\_name, dept\_location) is lossless join decomposition.

### Exercise:

A. Suppose R (v w x y z) and set of FDs

F : { z  $\rightarrow$  y,  
y  $\rightarrow$  z,  
x  $\rightarrow$  yv,  
vw  $\rightarrow$  x }

Which of the following decomposition is lossless, justify your answer:

1. R1(v w x), R2( x y z)
2. R1(v w), R2( y z)
3. R1(v w x), R2( y z)
4. R1(v w), R2( w x y z)

B. Suppose a relation R

A	B	C	D	E
p	111	6	a	x
q	134	5	b	y
p	338	6	c	z
r	463	4	d	w

Which of the following decomposition is lossless, justify your answer:

1.  $R_1(A\ B), R_2(C\ D)$
2.  $R_1(A\ B\ C), R_2(D\ E)$
3.  $R_1(A\ B\ C), R_2(C\ D\ E)$
4.  $R_1(A\ B\ C\ D), R_2(A\ C\ D\ E)$
5.  $R_1(A\ B\ C\ D), R_2(D\ E)$
6.  $R_1(A\ B\ C), R_2(B\ C\ D), R_3(D\ E)$

