

Course Name: **A Level (1st Sem)**

Subject : **Introduction to DBMS**

Topic: **DB Normalization – Dependency Preserving
Decomposition (Part 13)**

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Database Normalization – Dependency Preserving Decomposition

Suppose R is a relational schema and F is the set of functional dependencies on R.

If R is decomposed into relations R₁, R₂, R_n, each holding functional dependencies F₁, F₂, F_n respectively.

We can say, $F^{\sim} = F_1 \cup F_2 \cup \dots \cup F_n$

Now this decomposition will be considered as **dependency preserving decomposition** if and only if

Every dependency in F is logically implied by F^{\sim} i.e. $F^{\sim+} = F^+$

It is obvious that $F_1 \subseteq F^+$, $F_2 \subseteq F^+$, and so on

If we verify that F^{\sim} is satisfied in R, we have verified that decomposition is dependency preserving decomposition i.e. **$F_1 \cup F_2 = F$**

Suppose R (A B C D) and set of functional dependencies

F: AB \rightarrow CD

D \rightarrow A

If R is decomposed into following two relations

R₁ (A D),

R₂ (B C D)

Identify that this decomposition is dependency preserving or not?

Solution:

R (A B C D)

F: AB \rightarrow CD

D \rightarrow A

R1 (A D)

Since there are two attributes in R1 i.e. A, D

so find A^+ , D^+

[Closure must be calculated using FD set in R]

$A^+ = A$ [It concludes trivial FD $A \rightarrow A$]

$D^+ = AD$ [It concludes FD $D \rightarrow A$]

The closure of attributes concludes, following FD exist in R1

F1 { D \rightarrow A }

R2 (B C D)

Since there are three attributes in R2 i.e. B, C, D

so find B^+ , C^+ , D^+ , BC^+ , CD^+ , BD^+

[Closure must be calculated using FD set in R]

$B^+ = B$ [trivial]

$C^+ = C$ [trivial]

$D^+ = DA$ [It concludes FD, $D \rightarrow A$ but it is invalid FD for R2 because A is not attribute in R2]

$BC^+ = BC$ [trivial]

$CD^+ = CDA$ [It concludes FD, $CD \rightarrow A$ but it is invalid FD for R2 because A is not attribute in R2]

$BD^+ = BDAC$ [It concludes FD, $BD \rightarrow C$ A is not included at right side of FD because A is not attribute in R2]

The closure of attributes concludes, following FD exist in R2

F2 { BD \rightarrow C }

Now $F^+ = F1 \cup F2 = \{ D \rightarrow A, BD \rightarrow C \}$

and original F in R = { AB \rightarrow CD, D \rightarrow A }

It can be seen that while decomposing, the functional dependency $AB \rightarrow CD$ has been lost.

To understand, calculate $AB^+ = AB$ [Using FD in F^+] while in F , AB can determine CD but this dependency is lost in F^+ .

Therefore, **this decomposition is not dependency preserving decomposition.**

Exercise:

Suppose $R(A B C D)$ and set of functional dependencies

$F: AB \rightarrow C$

$C \rightarrow D$

$D \rightarrow A$

If R is decomposed into following two relations

$R_1(A B C),$

$R_2(C D)$

Identify that this decomposition is dependency preserving or not?

